



## **What is Fluency in Maths?**

Fluency in maths is about developing number sense and being able to use the most appropriate method for the task at hand; to be able to apply a skill to multiple contexts.

The National Curriculum states that pupils should become fluent in the fundamentals of mathematics through varied and frequent practice. While a part of this is about knowing key mathematical facts and recalling them efficiently, fluency means so much more than this as it allows pupils to delve much deeper.

But what are the stages our learners go through in order to become fluent? And how do we decide if a child has attained fluency in a mathematical concept?

### **Three stages of fluency**

#### **1. Simple strategies**

Initially, as a child gets to grips with a new skill, they can work out an answer using concrete resources or counting strategies. This will probably help them solve a problem accurately, but it's not the most efficient strategy.

#### **2. Mental calculations**

As learners become more proficient with new learning, they reach the second stage of fluency. Learners at this stage can work out an answer in their head. It still requires some thinking and effort as they develop reasoning strategies, but they're well on their way to becoming more efficient.

#### **3. Achieving fluency**

Finally, children reach the stage of 'I just knew it'. They can reliably produce accurate answers in an efficient way. This stage often involves using their knowledge flexibly; making connections so that the known can be used to work out the unknown.

## **How do we know when a learner is fluent?**

You can identify a fluent learner when they have a secure understanding of what they're doing and why they're doing it. Fluency is made up of three key parts: efficiency, accuracy and flexibility.

- Efficiency: learners choose efficient strategies and don't get bogged down in too many steps
- Accuracy: learners are accurate in their workings, have great recall of facts and double check their answers
- Flexibility: learners understand that there are many ways to solve a problem







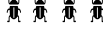



Fluency means that learners can do more than just memorise procedures. To be truly fluent, a child understands the meaning of the operations and their relationships to each other, they have a large knowledge bank of number facts, and a deep understanding of the base ten system.

## **How we build fluency in the classroom**


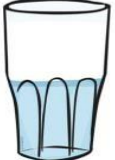
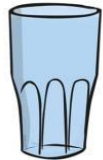
At Kildwick CE Primary School, each class uses knowledge organisers for their year groups to help direct the teaching of fluency. Teachers provide fluency activities (remembering red) on a daily or weekly basis and ensure there are visual reminders around the classroom to bring it to the forefront of the children's minds.

The relevant knowledge organisers are shared with parents, enabling parents to become involved in learning and have a greater understanding of the expectations in maths for their child. By the end of the year, children should know these facts and the aim is for them to achieve true automaticity so they can recall them instantly.

# FS Maths Knowledge Mat

Numbers To 20	Number bonds to 5					Quantity To 10				Months Of The Year		
1	1	2	3	4	5	1		6		January	February	March
2	0 + 1	0 + 2	0 + 3	0 + 4	0 + 5	2		7		April	May	June
3		1 + 1	1 + 2	1 + 3	1 + 4	3		8		July	August	September
4				2 + 2	2 + 3	4		9		October	November	December
5						5		10				
6												
7												
8												
9												
10												
11												
12												
13												
14												
15												
16												
17												
18												
19												
20												

Capacity		
Empty	Half Full	Full
		


  

Number	Double
0	0
1	2
2	4
3	6
4	8
5	10




  

Number	Half
0	0
2	1
4	2
6	3
8	4
10	5





  

Time	
	<b>O'clock</b> The hour hand points to the time and the minute hand points to 12.




  

Weight	
Heavy / Heavier / Heaviest	
Light / Lighter / Lightest	
Balanced / Equal	

Shapes		
circle		
triangle		
square		
rectangle		

Pattern		
Colour		blue, red, blue, red
Size		big, small, big, small
Length		long, short, long, short

Days of the Week
Monday
Tuesday
Wednesday
Thursday
Friday
Saturday
Sunday

# Year 1: Maths Knowledge Mat

Numerals and Number Vocabulary			
0	zero	10	ten
1	one	20	twenty
2	two	30	thirty
3	three	40	forty
4	four	50	fifty
5	five	60	sixty
6	six	70	seventy
7	seven	80	eighty
8	eight	90	ninety
9	nine	100	one hundred

Symbols and Vocabulary	
+	plus, add
-	minus, subtract
=	is equal to





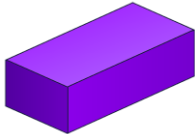



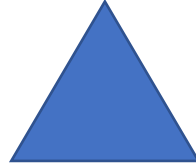

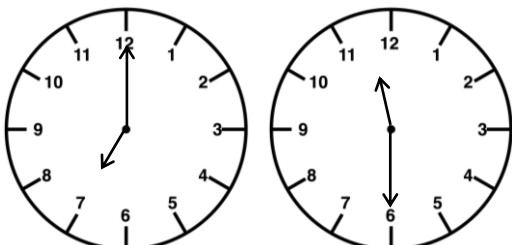
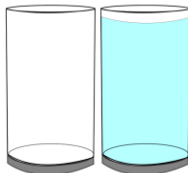
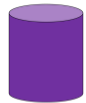


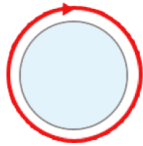
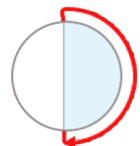
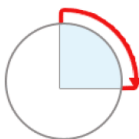

Odd and Even
<b>Odd</b> numbers end in 1, 3, 5, 7, 9
<b>Even</b> numbers end in 2, 4, 6, 8, 0

Counting
Count forwards and backwards from <b>any number to and across 100</b>
Count in <b>2s</b> 2, 4, 6, 8, 10, 12...
Count in <b>5s</b> 5, 10, 15, 20, 25, 30...
Count in <b>10s</b> 10, 20, 30, 40, 50 ...
Say the number <b>one more than...</b>
Say the number <b>one less than...</b>

Doubles, halves and quarters		
Number	double	quarter
6	12	
7	14	
8	16	2
9	18	
10	20	
Number	half	quarter
12	6	3
14	7	
16	8	4
18	9	
20	10	5

Number bonds within 20	
1	1+0
2	2+0 1+1
3	3+0 2+1
4	4+0 3+1 2+2
5	5+0 4+1 3+2
6	6+0 5+1 4+2 3+3
7	7+0 6+1 5+2 4+3
8	8+0 7+1 6+2 5+3 4+4
9	9+0 8+1 7+2 6+3 5+4
10	10+0 9+1 8+2 7+3 6+4 5+5
11	11+0 10+1 9+2 8+3 7+4 6+5
12	12+0 11+1 10+2 9+3 8+4 7+5 6+6
13	13+0 12+1 11+2 10+3 9+4 8+5 7+6
14	14+0 13+1 12+2 11+3 10+4 9+5 8+6 7+7
15	15+0 14+1 13+2 12+3 11+4 10+5 9+6 8+7
16	16+0 15+1 14+2 13+3 12+4 11+5 10+6 9+7 8+8
17	17+0 16+1 15+2 14+3 13+4 12+5 11+6 10+7 9+8 8
18	18+0 17+1 16+2 15+3 14+4 13+5 12+6 11+7 10+8
19	19+0 18+1 17+2 16+3 15+4 14+5 13+6 12+7 11+8 10+9
20	20+0 19+1 18+2 17+3 16+4 15+5 14+6 13+7 12+8 11+9 10+10

# Year 1: Maths Knowledge Mat

Time – Sticky Knowledge		Key Vocabulary - Measurement		2D Shapes	3D Shapes		
There are <b>24 hours in a day</b>		long / short longer / shorter tall / short double / half 		square 	cube 		
There are <b>60 minutes in an hour</b>				rectangle 	cuboid 		
There are <b>60 seconds in a minute</b>		heavy / light heavier than... lighter than... 		circle 	sphere 		
<b>A.M.</b> means in the morning <b>P.M.</b> means in the afternoon				triangle 	cone 		
<b>O'Clock</b> is when the minute hand points to the 12 and the hour hand points at the hour. <b>Half past</b> is when the minute hand points to the six and the hour hand points past the hour.  Seven o'clock      Half past eleven		full / empty more than... less than... half full / half empty 		cylinder 	pyramid 		
quicker / slower before / after first / next today / yesterday morning / afternoon / evening 		Direction and Movement					
<b>Days of the Week</b> Monday Tuesday Wednesday Thursday Friday Saturday Sunday		<b>Months of the Year</b> January      July February      August March      September April      October May      November June      December		Whole turn 	Half turn 	Quarter turn 	Three- quarter turn 

# Year 2: Maths Knowledge Mat

## Read and write numbers to at least 100 in numerals and in words

0	zero	10	ten
1	one	20	twenty
2	two	30	thirty
3	three	40	forty
4	four	50	fifty
5	five	60	sixty
6	six	70	seventy
7	seven	80	eighty
8	eight	90	ninety
9	nine	100	one hundred

## Symbols and Vocabulary

<b>x</b>	multiply, times
<b>÷</b>	divide
<b>&lt;</b>	is less than
<b>&gt;</b>	is greater than
<b>=</b>	is equal to

## Counting to at least 100

Count forwards and backwards from **any number in steps of 2**

Count forwards and backwards from **any number in steps of 3**

Count forwards and backwards from **any number in steps of 5**

Count forwards and backwards from **any number in steps of 10**

**Addition and multiplication can be done in any order. But subtraction and division can not!**

$$23 + 11 = 34 \quad 11 + 23 = 34$$

$$3 \times 5 = 15 \quad 5 \times 3 = 15$$

$23 - 11 = 12$   
But you can not take 23 coins from 11 coins

$$10 \div 5 = 2 \quad 5 \div 10 = \frac{1}{2}$$

**Using knowledge of number bonds within 20 (from Year 1) to calculate to at least 100**

Examples:

If  $3 + 7 = 10$  then  $30 + 70 = 100$

If  $6 - 4 = 2$  then  $60 - 40 = 20$

## Multiplication Tables

x	2	5	10
1	2	5	10
2	4	10	20
3	6	15	30
4	8	20	40
5	10	25	50
6	12	30	60
7	14	35	70
8	16	40	80
9	18	45	90
10	20	50	100
11	22	55	110
12	24	60	120

## Fractions

$\frac{1}{2}$	a half
$\frac{1}{4}$	a quarter
$\frac{3}{4}$	three quarters
$\frac{1}{2} =$ two quarters	
You can calculate fractions of numbers:	
$\frac{1}{2}$ of 20 is 10. This is the same as dividing 20 by 2.	
$\frac{1}{4}$ of 20 is 5. This is the same as dividing 20 by 4.	

2 Digit Place value	Tens	Ones
Example 56 is	5	6
99	9	9
7	0	7

# Year 2: Maths Knowledge Mat

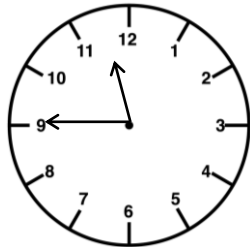
## Time – Sticky Knowledge

There are **24 hours in a day**

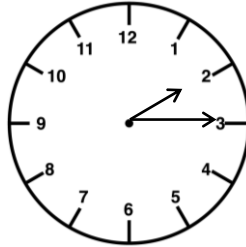
There are **60 minutes in an hour** and a **clock shows these in 5 minute intervals**

**Quarter to** is when the minute hand points to the 9 and the hour hand nearly points at the hour.

**Quarter past** is when the minute hand points to the three and the hour hand points past just the hour.



Quarter to 12



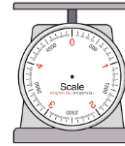
Quarter past 2

## Key Vocabulary - Measurement

Metre m  
Centimetre cm



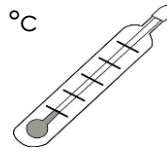
Kilogram kg  
Gram g



Litre l  
Millilitre ml



Degrees centigrade °C



## 2D Shapes

Quadrilaterals have four sides



Parallelogram



Isosceles Trapezoid



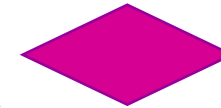
Rectangle



Square



Trapezoid

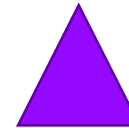


Rhombus



Kite

A polygon is a 2D shape with straight sides



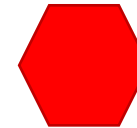
Triangle



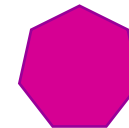
Quadrilateral



Pentagon



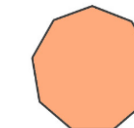
Hexagon



Heptagon



Octagon



Nonagon



Decagon

## Coins

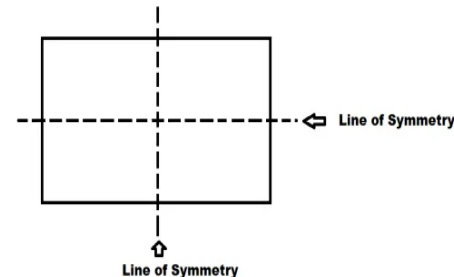
Pounds £



Pence p

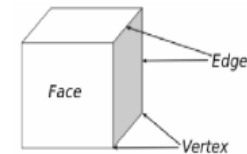


## Symmetry



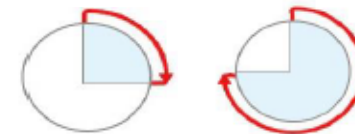
## 3D Shapes

Faces, edges and vertices



## Direction

Quarter turn is 1 right angle  
 $\frac{3}{4}$  turn is 3 right angles

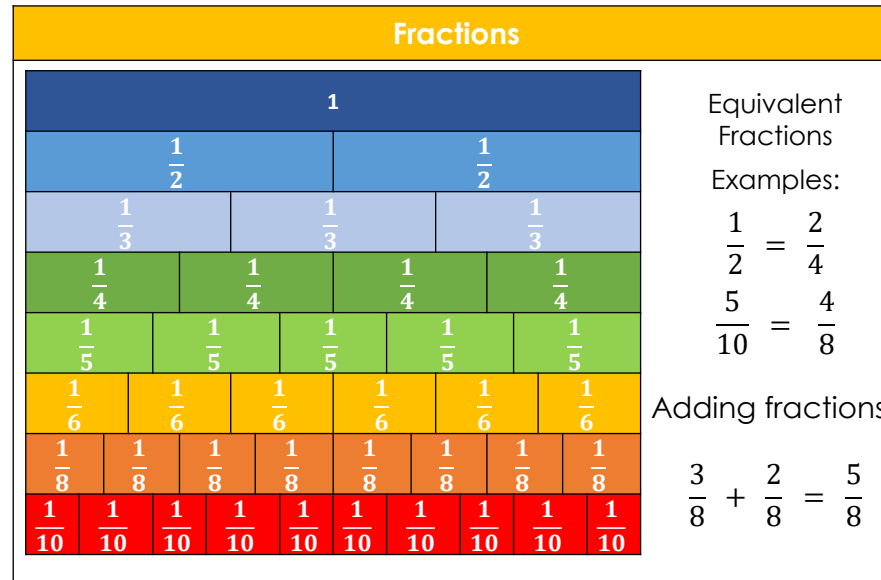


# Year 3: Maths Knowledge Mat

Counting from 0
Counting in <b>multiples of 4</b> 0, 4, 8, 12, 16, 20, 24, 28, 32...
Counting in <b>multiples of 8</b> 0, 8, 16, 24, 32, 40, 48...
Counting in <b>multiples of 50</b> 0, 50, 100, 150, 200, 250, 300...
Counting in <b>multiples of 100</b> 0, 100, 200, 300, 400, 500...

Vocabulary	
<b>100</b>	<b>hundred</b>
<b>1000</b>	<b>thousand</b>
<b>+</b> <b>-</b> <b>X</b> <b>÷</b>	<b>inverse operations</b>
$\frac{1}{2}$ ←	<b>Numerator</b>
$\frac{1}{2}$ ←	<b>Denominator</b>

Place value	Thousands	Hundreds	Tens	Ones		Tenths
1238	1	2	3	8	.	0
58.9	0	0	5	8	.	9
3050.4	3	0	5	0	.	4



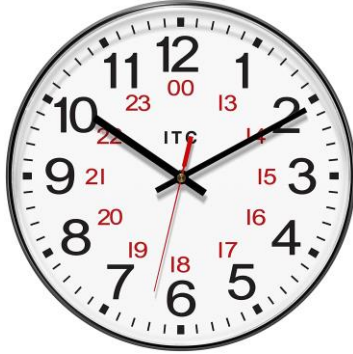
Multiplication Tables			
x	3	4	8
1	3	4	8
2	6	8	16
3	9	12	24
4	12	16	32
5	15	20	40
6	18	24	48
7	21	28	56
8	24	32	64
9	27	36	72
10	30	40	80
11	33	44	88
12	36	48	96

Formal methods of addition, subtraction and short multiplication and division				
768 + 653 becomes $\begin{array}{r} 768 \\ + 653 \\ \hline 1421 \\ 11 \end{array}$	862 - 514 becomes $\begin{array}{r} 862 \\ - 514 \\ \hline 348 \end{array}$	934 - 456 becomes $\begin{array}{r} 934 \\ - 456 \\ \hline 478 \end{array}$	26 x 8 becomes $\begin{array}{r} 26 \\ \times 8 \\ \hline 208 \\ 4 \end{array}$	78 ÷ 6 becomes $\begin{array}{r} 13 \\ 6 \overline{) 78} \\ \underline{6} \phantom{0} \\ 18 \\ \underline{18} \\ 0 \end{array}$

# Year 3: Maths Knowledge Mat

## Time – Sticky Knowledge

### 24 hour clocks



The time is 10.10 in the morning or 22.10 in the evening in 24 hour time.

### Roman numerals



This clock is showing X to II or 10 to 2.  
On some clocks the 4 is IIII and sometimes it is IV

**a.m.** is from **midnight** until mid-day (noon)  
1 to 12 in 24 hour clock time

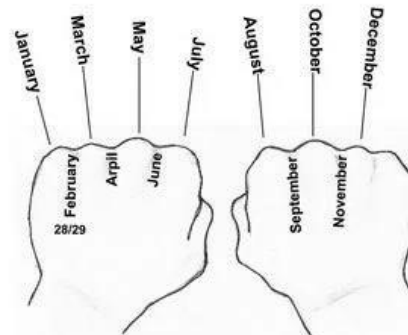
**p.m.** is from mid-day (**noon**) until midnight  
13 to 24 in 24 hour clock time

There are **365 days in a year.**

**A leap year has 366 days.** This is February 29<sup>th</sup> and happens every 4 years.

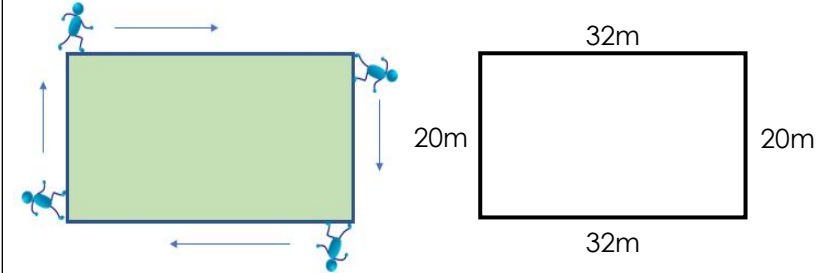
<b>January</b>	31 days
<b>February</b>	28 days
<b>March</b>	31 days
<b>April</b>	30 days
<b>May</b>	31 days
<b>June</b>	30 days
<b>July</b>	31 days
<b>August</b>	31 days
<b>September</b>	30 days
<b>October</b>	31 days
<b>November</b>	30 days
<b>December</b>	31 days

### 'Knuckle Mnemonic'



## Perimeter

Perimeter is the distance around a 2D shape



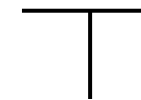
## Non symmetrical (irregular) polygons

Polygon/Shape	Regular	Irregular
Triangle		
Quadrilateral		
Pentagon		
Hexagon		
Heptagon		
Octagon		

## Lines

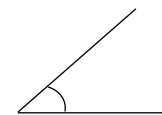


Parallel



Perpendicular

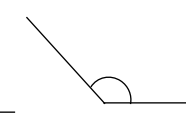
## Angles



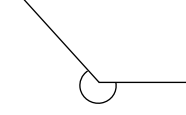
**Acute angle**  
Less than 90°



**Right angle**  
Exactly 90°



**Obtuse angle**  
More than 90°  
Less than 180°



**Reflex angle**  
More than 180°  
Less than 360°

# Year 4: Maths Knowledge Mat

Counting from 0
Counting in <b>multiples of 6</b> 0, 6, 12, 18, 24, 30, 36, 42 ...
Counting in <b>multiples of 7</b> 0, 7, 14, 21, 28, 35, 42, 49...
Counting in <b>multiples of 9</b> 0, 9, 18, 27, 36, 45, 54, 63 ...
Counting in <b>multiples of 25</b> 0, 25, 50, 75, 100, 125, 150...
Counting in <b>multiples of 1000</b> 0, 1000, 2000, 3000, 4000...
Counting up and down in <b>hundredths</b> $\frac{1}{100}, \frac{2}{100}, \frac{3}{100}, \frac{4}{100} \dots \frac{99}{100}, 1$
A <b>thousand more</b> than 4753 is 5753. A <b>thousand less</b> than 4753 is 3753.

Rounding
<p>The numbers below half way all <b>ROUND DOWN</b> to 30</p> <p>The numbers above half way all <b>ROUND UP</b> to 40</p> <p>The number in the middle is half way and <b>ROUNDS UP</b> to 40</p> <p><b>Rounding to 100 and 1000</b> follows the same rule. 350 rounds up to 400 3500 rounds up to 4000</p> <p><b>Rounding decimal places</b> also follows the same rule. 3.4 rounds to 3.0 but 3.5 rounds to 4.0 3.04 rounds to 3.00 but 3.05 rounds to 3.10</p>

Negative Numbers
<p>Numbers above 0 (zero) are positive</p> <p>Numbers below 0 (zero) are negative</p>

Multiplication Tables (and 2x, 3x, 4x, 5x, 8x, 10x from previous years)					
x	6	7	9	11	12
1	6	7	9	11	12
2	12	14	18	22	24
3	18	21	27	33	36
4	24	28	36	44	48
5	30	35	45	55	60
6	36	42	54	66	72
7	42	49	63	77	84
8	48	56	72	88	96
9	54	63	81	99	108
10	60	70	90	110	120
11	66	77	99	121	132
12	72	84	108	132	144

Formal methods of short multiplication and division	
351 x 7 becomes	91 ÷ 7 becomes
<div><div>351</div><div>x</div><div>7</div><div><div>2457</div><div>23</div></div></div>	<div><div>13</div><div>7</div><div>2</div><div>91</div></div>

Roman Numerals
1 = I      10 = X 2 = II     20 = XX 3 = III    30 = XXX 4 = IV     40 = XL 5 = V      50 = L 6 = VI     60 = LX 7 = VII    70 = LXX 8 = VIII   80 = LXXX 9 = IX     90 = XC 100 = C

Factors
A <b>factor pair</b> is a pair of numbers that, when multiplied will result in a given product.  Factor pairs of 16 are 1, 16 2, 8 4, 4

# Year 4: Maths Knowledge Mat

## Time – Sticky Knowledge

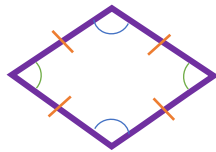
### Digital and analogue clocks



Both clocks show it is 10 o'clock. But only the digital clock shows that it is pm (in the evening) because it is using 24 hour time.

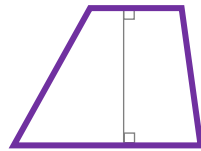
## 2D Shapes

### Rhombus



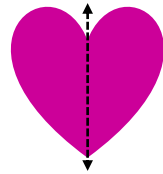
All four sides are the same length, like a square that has been squashed sideways.

### Trapezium (or trapezoid)

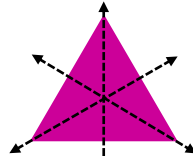


Two sides are parallel. Side lengths and angles are not equal.

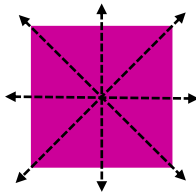
## Symmetry



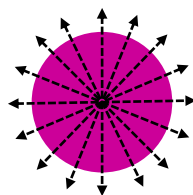
1 line of symmetry



3 lines of symmetry



4 lines of symmetry



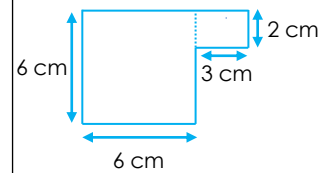
Infinite number of lines of symmetry

## Simplifying fractions

$$\frac{40}{80} = \frac{20}{40} = \frac{10}{20} = \frac{5}{10} = \frac{1}{2} \quad \text{So } \frac{40}{80} = 0.5$$

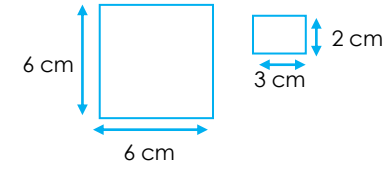
## Area

The area of this shape → EQUALS → the area of these two



The area of this shape

6



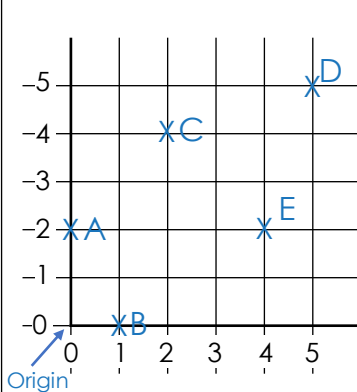
$$= (6 \times 6) + (2 \times 3) \\ = 36 + 6 \\ = 42$$

## Place value

Each row divides by 10

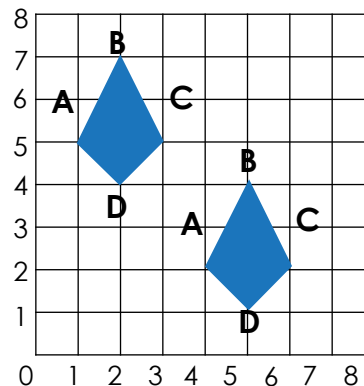
Place value	Tens	Ones	•	tenths	hundredths
45	4	5	•	0	0
$4.5 = 4\frac{5}{10} = 4\frac{1}{2}$	0	4	•	5	0
$0.45 = \frac{45}{100}$	0	0	•	4	5

## Coordinates



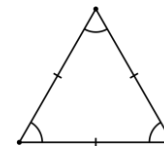
X axis comes first, so

A = (0,2)  
B = (1,0)  
C = (2,4)  
D = (5,5)  
E = (4,2)

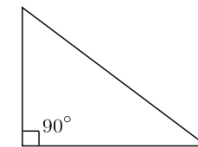


This shape has been **translated** up and left by -3, -3. (Taken away from each co-ordinate.)

## Triangles



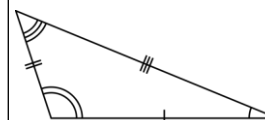
Equilateral Triangle



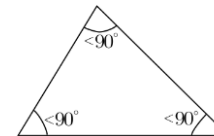
Right Triangle



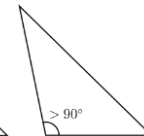
Isosceles Triangle



Scalene Triangle



Acute Triangle



Obtuse Triangle

# Year 5: Maths Knowledge Mat

## Rounding

**78,543**

To the **nearest 10** is 78,540  
 To the **nearest 100** is 78,500  
 To the **nearest 1000** is 79,000  
 To the **nearest 10,000** is 80,000  
 To the **nearest 100,000** is 100,000

**67.53**

To the **nearest 10** is 70  
 To the **nearest whole number** is 68  
 To **one decimal place** is 67.6

## Multiplying a fraction by a whole number

If you have a **proper** fraction multiplied by a whole number, it is going to be **less** than that whole number

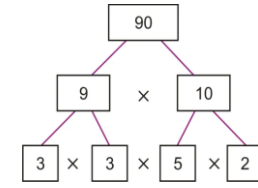
$$\frac{3}{5} \times 2$$

$$\frac{3}{5} \times \frac{2}{1} = \frac{6}{5} = 1 \frac{1}{5}$$

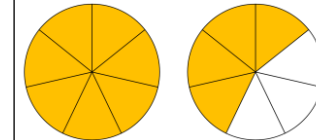
## Prime Numbers

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

## Prime factors



## Converting a mixed number to an improper fraction



$$1\frac{4}{7} = \frac{11}{7}$$

## Place value

Each row divides by 10

	Tens	Ones	.	tenths	hundredths	thousandths
36.7	3	6	.	7	0	0
3.67	0	3	.	6	7	0
0.367	0	0	.	3	6	7

$$36.7 = 36\frac{7}{10}$$

$$3.67 = 3\frac{67}{100}$$

$$0.367 = \frac{367}{1000}$$

## Percentages %

'part per hundred'  $50\% = \frac{50}{100}$   $25\% = \frac{25}{100}$

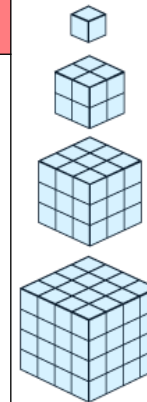
50% of 100 = 50    25% of 100 = 25  
 50% of 200 = 100    25% of 200 = 50  
 50% of 300 = 150    25% of 300 = 75

$$\frac{1}{2} = 0.5 = 50\% \quad \frac{1}{4} = 0.25 = 25\%$$

$$\frac{1}{5} = 0.2 = 20\% \quad \frac{2}{5} = 0.4 = 40\%$$

## Square and cubed numbers

$$\begin{aligned} 1^2 &= 1 \times 1 = 1 \\ 2^2 &= 2 \times 2 = 4 \\ 3^2 &= 3 \times 3 = 9 \\ 4^2 &= 4 \times 4 = 16 \\ 5^2 &= 5 \times 5 = 25 \\ 6^2 &= 6 \times 6 = 36 \\ 7^2 &= 7 \times 7 = 49 \\ 8^2 &= 8 \times 8 = 64 \\ 9^2 &= 9 \times 9 = 81 \\ 10^2 &= 10 \times 10 = 100 \end{aligned}$$



1 is the first cube number,  
because  $1 \times 1 \times 1 = 1$

8 is the second cube number,  
because  $2 \times 2 \times 2 = 8$

27 is the third cube number,  
because  $3 \times 3 \times 3 = 27$

64 is the fourth cube number,  
because  $4 \times 4 \times 4 = 64$

## Formal methods of multiplication and division

3741 x 6 becomes

$$\begin{array}{r} 3741 \\ \times 6 \\ \hline 22446 \\ 42 \end{array}$$

485 ÷ 11 becomes

$$\begin{array}{r} 44 \text{ r}1 \\ 11 \overline{) 485} \\ \underline{44} \phantom{0} \\ 45 \phantom{0} \\ \underline{44} \phantom{0} \\ 10 \phantom{0} \\ \underline{11} \phantom{0} \\ 10 \phantom{0} \\ \underline{11} \phantom{0} \\ 10 \phantom{0} \\ \underline{11} \phantom{0} \\ 10 \phantom{0} \\ \underline{11} \phantom{0} \\ 10 \phantom{0} \end{array}$$

34 x 26 becomes

$$\begin{array}{r} 34 \\ \times 26 \\ \hline 204 \\ 680 \\ \hline 884 \end{array}$$

134 x 27 becomes

$$\begin{array}{r} 134 \\ \times 27 \\ \hline 938 \\ 2680 \\ \hline 3618 \end{array}$$

# Year 5: Maths Knowledge Mat

## Measures – Sticky Knowledge



1 km = 1000 m  
1 m = 100 cm  
1 cm = 10 mm



1 kg = 1000 g



1 l = 1000 ml

### Imperial measures

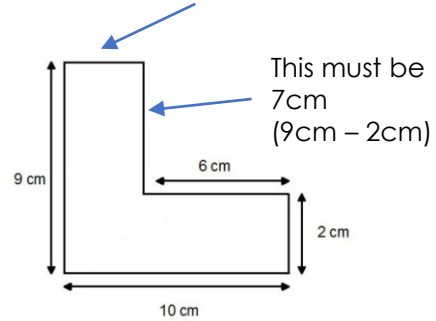
1 mile = 1.6 km  
1 yard = 0.91 m  
1 foot = 30 cm  
1 inch = 2.54 cm

1 lb (pound) = 0.45 kg

1 pint = 0.57 litre

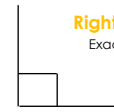
## Perimeter

This must be 4 cm (10cm – 6cm)



## Angles

**Right angle**  
Exactly 90°



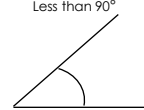
**Straight line**  
= 180°



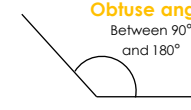
**Complete turn**  
= 360°



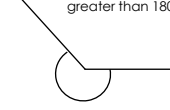
**Acute angle**  
Less than 90°



**Obtuse angle**  
Between 90° and 180°



**Reflex angle**  
greater than 180°



## 3D Shapes

Solid (3D) shapes are three-dimensional shapes having length, breadth and height.

### Examples



sphere



cone



cylinder



cube

### Prisms



triangular prism



square prism



rectangular prism



pentagonal prism



hexagonal prism



octagonal prism

### Pyramids



triangular pyramid



square pyramid



rectangular pyramid



pentagonal pyramid



hexagonal pyramid



octagonal pyramid

### Platonic solids



tetrahedron



cube



octahedron



dodecahedron



icosahedron

## Roman Numerals

Symbol	Value
I	1
V	5
X	10
L	50
C	100
D	500
M	1000

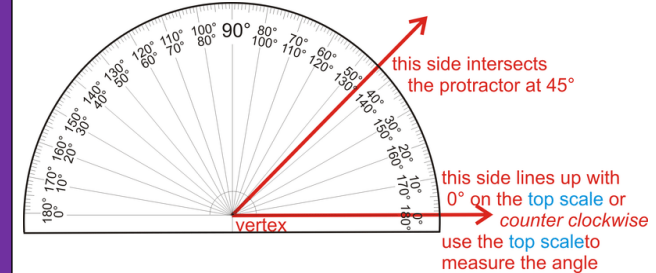
### Dates

2020 = MMXX  
2021 = MMXXI  
2022 = MMXXII  
2023 = MMXXIII  
2024 = MMXXIV

1066 = MLXVI

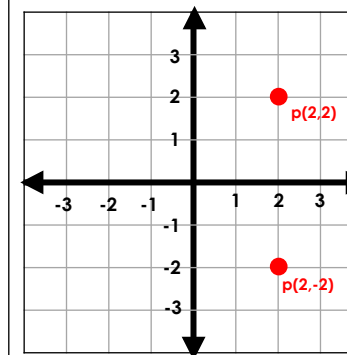
1939 = MCMXXXIX

## Using a protractor

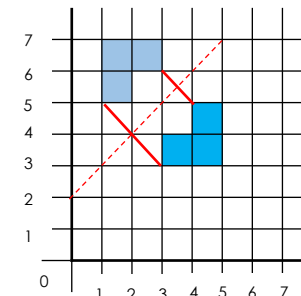


## Coordinates

P has been reflected in the x axis



The shape has been reflected in the dotted line  $y=x+2$



# Year 6: Maths Knowledge Mat

## Rounding

**8,378,543**

To the **nearest 10,000** is 8,380,000  
 To the **nearest 100,000** is 8,400,000  
 To the **nearest 1,000,000** is 8,000,000  
 To the **nearest 10,000,000** is 10,000,000

## Multiplying a fraction by a fraction

$$\frac{3}{5} \times \frac{6}{8} = \frac{3 \times 6}{5 \times 8} = \frac{18}{40}$$

$$\frac{3}{4} \times \frac{1}{3} = \frac{3 \times 1}{4 \times 3} = \frac{3}{12} = \text{reduces to } \frac{1}{4}$$

## Percentages

### On a calculator

36% of 76  
 $0.36 \times 76$

Change to a decimal and multiply

### Increasing

Increase £70 by 14%  
 $14\% \text{ of } 70 = 0.14 \times 70 = £9.80$   
 New amount = £70 + £9.80 = £79.80

### Fraction to %

$$\frac{15}{20} = \frac{75}{100} = 75\%$$

Or  $15 \div 20 \times 100 = 75\%$

### Decreasing

Decrease £70 by 14%  
 $14\% \text{ of } 70 = 0.14 \times 70 = £9.80$   
 New amount = £70 - £9.80 = £60.20

### Without a calculator

50% - half  
 25% - half and half  
 75% - 50% + 25%

10% - divide by 10  
 5% - half 10%  
 20% - double 10%

## Calculations with mixed numbers

### Add Mixed Numbers

$$8\frac{1}{2} + 3\frac{3}{4}$$

$$= \frac{17}{2} + \frac{15}{4}$$

Change to improper fractions

$$= \frac{17 \times 2}{2 \times 2} + \frac{15}{4}$$

Change to common denominator

$$= \frac{34}{4} + \frac{15}{4}$$

$$= \frac{49}{4}$$

Add the numerators

$$= 12\frac{1}{4}$$

Change to mixed numbers

### Subtract Mixed Numbers

$$8\frac{1}{2} - 4\frac{3}{4}$$

$$= \frac{17}{2} - \frac{15}{4}$$

Change to improper fractions

$$= \frac{17 \times 2}{2 \times 2} - \frac{15}{4}$$

Change to common denominator

$$= \frac{34}{4} - \frac{15}{4}$$

$$= \frac{19}{4}$$

Subtract the numerators

$$= 4\frac{3}{4}$$

Change to mixed numbers

## Adding fractions

$$\frac{1}{2} + \frac{1}{3} = ?$$

$$\frac{1}{2} \times \frac{3}{3} = \frac{3}{6} \quad \frac{1}{3} \times \frac{2}{2} = \frac{2}{6}$$

$$\frac{3}{6} + \frac{2}{6} = \frac{5}{6}$$

## Mean Average

The sum of all data points divided by the number of data points

## Formal methods of multiplication and division

134 x 27 becomes

$$\begin{array}{r} \phantom{0}2 \phantom{0}2 \\ 134 \\ \times \phantom{0}27 \\ \hline 2680 \\ 938 \phantom{0} \\ \hline 3618 \phantom{0} \\ \phantom{0}1 \phantom{0}1 \end{array}$$

564 ÷ 15 becomes

$$\begin{array}{r} 15 \overline{) 564} \\ \underline{45} \phantom{0} \\ 114 \\ \underline{105} \\ 9 \phantom{0} \\ \underline{9} \phantom{0} \\ 0 \end{array} \quad \begin{array}{l} 15 \times 30 \\ 15 \times 7 \end{array}$$

$$\frac{9}{15} = \frac{3}{5}$$

Answer:  $37\frac{3}{5}$

432 ÷ 15 becomes

$$\begin{array}{r} \phantom{0}2 \phantom{0}8 \phantom{0}8 \\ 15 \overline{) 432} \\ \underline{30} \phantom{0} \\ 132 \\ \underline{120} \\ 120 \\ \underline{120} \\ 0 \end{array}$$

Answer: 28.8

384 ÷ 11 becomes

$$\begin{array}{r} \phantom{0}3 \phantom{0}4 \phantom{0}r10 \\ 11 \overline{) 384} \\ \underline{33} \phantom{0} \\ 54 \\ \underline{55} \\ -1 \end{array}$$

Answer:  $34\frac{10}{11}$

## BODMAS

B → Bracket  
 O → Of  
 D → Division  
 M → Multiplication  
 A → Addition  
 S → Subtraction

### BODMAS EXAMPLE

$$40 - (5 \times 2^2 + 7)$$

Brackets 1<sup>st</sup> then use ODMAS inside the brackets

$$40 - (5 \times 4 + 7) \quad (2^2)$$

$$40 - (20 + 7) \quad (\text{Multiply } 5 \times 4)$$

$$40 - 27 \quad (\text{Add } 20 + 7)$$

Answer = 13

## Ratio

**Ratio** compares values.  
 A **ratio** says how much of one thing there is compared to another thing.  
**Ratio 3:1.** There are 3 blue squares to 1 yellow square.

# Year 6: Maths Knowledge Mat

## Algebra

One step equation e.g.  
 $+ 14 = 20$

Undo addition or subtraction  $- 14 - 14$

$$y = 6$$

Two step equation e.g.  
 $+ 5 = 11$

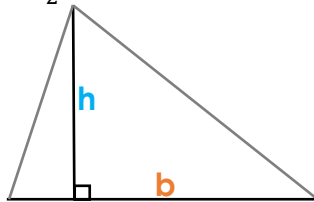
Undo addition or subtraction  $- 5 - 5$

$$2x = 6$$

Undo multiplication or division  $\div 2 \div 2$

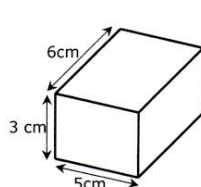
## Area of a triangle

$$\text{Area} = \frac{1}{2} \times b \times h = \frac{bh}{2}$$

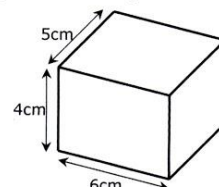


## Volume

volume = length x width x height

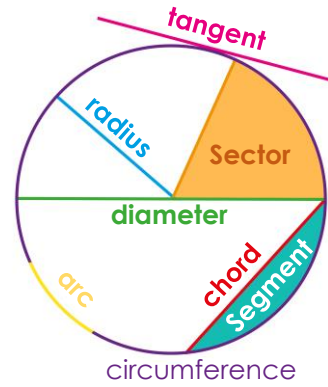


$$\text{volume} = 6 \times 5 \times 3 = 90 \text{ cm}^3$$



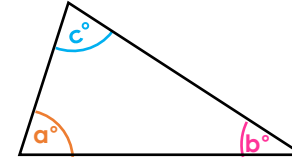
$$\text{volume} = 5 \times 6 \times 4 = 120 \text{ cm}^3$$

## Circles

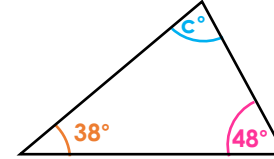


The **diameter** is twice the **radius**

## Angles in a triangle



$$a^\circ + b^\circ + c^\circ = 180^\circ$$



$$38^\circ + 60^\circ + c^\circ = 180^\circ$$

$$c^\circ = 180^\circ - 98$$

$$c^\circ = 82^\circ$$

## Nets of 3D shapes

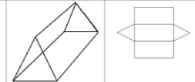
Cube



Cuboid



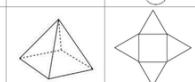
Triangular Prism



Cylinder



Pyramid



## Square Numbers

$$1^2$$

$$1$$

## Square Roots

$$\sqrt{1}$$

$$1$$

$$2^2$$

$$4$$

$$\sqrt{4}$$

$$2$$

$$3^2$$

$$9$$

$$\sqrt{9}$$

$$3$$

$$4^2$$

$$16$$

$$\sqrt{16}$$

$$4$$

$$5^2$$

$$25$$

$$\sqrt{25}$$

$$5$$

$$6^2$$

$$36$$

$$\sqrt{36}$$

$$6$$

$$7^2$$

$$49$$

$$\sqrt{49}$$

$$7$$

$$8^2$$

$$64$$

$$\sqrt{64}$$

$$8$$

$$9^2$$

$$81$$

$$\sqrt{81}$$

$$9$$

$$10^2$$

$$100$$

$$\sqrt{100}$$

$$10$$

$$11^2$$

$$121$$

$$\sqrt{121}$$

$$11$$

$$12^2$$

$$144$$

$$\sqrt{144}$$

$$12$$

$$13^2$$

$$169$$

$$\sqrt{169}$$

$$13$$

## Cube Numbers

$$1^3$$

$$1$$

## Cube Roots

$$\sqrt[3]{1}$$

$$1$$

$$2^3$$

$$8$$

$$\sqrt[3]{8}$$

$$2$$

$$3^3$$

$$27$$

$$\sqrt[3]{27}$$

$$3$$

$$4^3$$

$$64$$

$$\sqrt[3]{64}$$

$$4$$

$$5^3$$

$$125$$

$$\sqrt[3]{125}$$

$$5$$

## Vocabulary

**factors**

numbers that you multiply together to get other numbers

**multiple**

the result of multiplying a number by an integer

**HCF**

**Highest Common Factor** - the largest factor shared by two or more numbers

**LCM**

**Lowest Common Multiple** - the smallest number that is a multiple of two or more numbers.